Rectifier effect in an atmospheric model with daily biospheric fluxes: impact on inversion calculation

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ABSTRACT
Atmospheric CO2 measurements show strong synoptic variability. To understand the contribution of the synoptic signals on atmospheric CO2 inversion, we simulate the cases of biospheric fluxes with and without synoptic variations (referred to as ‘Synoptic’ and ‘Reference’, respectively) using an atmospheric transport model, and then perform inversion analyses with these biospheric CO2 concentration fields.

Results show the monthly and annually averaged CO2 concentration anomalies (Synoptic–Reference) are functions of the distance from the continental biospheric source regions. Remote sites (like Mauna Loa) show averaged monthly amplitude of ∼0.2 ppm, while continental sites show averaged monthly amplitudes of 1–2 ppm with maximum monthly amplitudes up to 7 ppm. Spatial scales of these monthly mean synoptic anomaly patterns may exceed 1000 km. These CO2 concentration patterns are the results of the interaction of the synoptic CO2 flux field and atmospheric transport, and may be referred to as the synoptic Rectifier Effect.

Inversion CO2 fluxes for 1992–1995 are obtained using biospheric background fields with and without synoptic biospheric flux variations. The maximum magnitude differences in estimated monthly flux for land and ocean regions are ∼0.4 and ∼0.2 GtC month−1, respectively. The average land sink increases by 0.19 GtC yr−1 while the average ocean sink decreases by 0.30 GtC yr−1.

1. Introduction
Inversion of atmospheric CO2 concentration (mixing ratio) measurements to estimate spatial and temporal distributions of CO2 sources/sinks has become a popular scientific endeavour (e.g. Rayner et al., 1999; Gurney et al., 2002, 2004; Baker et al., 2006). This scientific activity constitutes an important investigation in trying to understand the processes and mechanisms controlling CO2 sources/sinks distribution within the global carbon cycle, both in time and space. However, we are faced with an underdetermined problem because we do not have sufficient number of observations to constrain the spatial-temporal distribution of CO2 fluxes to the atmosphere uniquely (Enting, 2002). In order to overcome this deficiency of available atmospheric CO2 measurement, it has been a typical practice to include some a priori information about the carbon cycle system so that the inverse solution would be consistent with our prior knowledge of the system.

In this Bayesian synthesis inverse approach (Tarantola, 1987; Rayner et al., 1999) used here, we generate an atmospheric background CO2 concentration field by assigning CO2 surface flux distribution for an atmospheric transport model. The flux distribution, both in time and space, includes contributions from fossil fuel combustion, ocean and terrestrial biosphere. These background values are subtracted from the observed CO2 concentrations at individual monitoring sites, with the residual allocated in an optimized way to various source regions as net CO2 fluxes in accordance with a set of response function. Each response function represents the resultant temporal evolution of CO2 concentration at a measurement site in response to the release of a unit CO2 flux from a basis region. A response function is essentially a ‘source–receptor’ relationship.

In TransCom 3 Level 1 (Gurney et al., 2002) and TransCom 3 Level 2 (Gurney et al., 2004), global distributions of annual mean and monthly mean carbon sources and sinks were estimated, respectively, averaged over the period 1992–1996. In both studies, net carbon fluxes were estimated for 11 land and 11 ocean regions. For the background field, fluxes from the 1990 and 1995 fossil fuel emissions (Andres et al., 1996; Brenkert, 1998), seasonally varying air–sea flux (Takahashi et al., 1999) and an
annually balanced monthly net CO$_2$ flux from a global terrestrial ecosystem model (the CASA model, Randerson et al., 1997) were used. In this study, we investigate the impact on inverse flux estimates of using annually balanced monthly net terrestrial biospheric flux in generating the background field.

Chan et al. (2004) showed that the atmosphere–biosphere exchange of CO$_2$ is accomplished by processes on various timescales. They identified the significance of synoptic and mesoscale processes in transporting biospheric CO$_2$ flux signal into the troposphere. (Typical synoptic scale processes include cyclones and anticyclones with horizontal spatial scale of ∼1000 km and timescale of ∼5–10 d. Typical mesoscale processes include thunderstorms and rainbands with horizontal spatial scale of ∼10–100 km and timescale of ∼0.1–1 d.) The atmosphere–biosphere interaction on a daily timescale (by synoptic and mesoscale processes including fronts and cyclones) was shown to be important, with possible impact on Rectifier Effect (Denning et al., 1995, 1996a,b). The Rectifier Effect is typically defined as the annual time-mean spatial CO$_2$ concentration gradient in the atmosphere caused by a covariance between the annually neutral biospheric CO$_2$ flux and the atmospheric transport. For example, the seasonal Rectifier Effect in the typical transport model is the annual time-mean spatial CO$_2$ concentration gradient in the atmosphere caused by the monthly varying biospheric CO$_2$ flux. However, other rectification processes are possible, for example, Gurney et al. (2005) investigated the possible rectification from seasonal variations in the fossil fuel sources.

In this study, using the National Institute of Environmental Studies (NIES) atmospheric transport model (Maksyutov and Inoue, 2000) and Biome-BioGeochmical Cycles (Biome-BGC) biospheric model (Thornton et al., 2002; Fujita et al., 2003), the contribution of daily atmosphere–biosphere interaction to the monthly to annually averaged CO$_2$ concentrations are characterized spatiotemporally by comparing the model simulated CO$_2$ concentrations with CO$_2$ fluxes varying on daily versus monthly time steps. Then, the effects of the daily CO$_2$ flux and atmospheric transport on time-dependent inverse flux estimates are investigated by comparing inversions with daily and monthly biospheric CO$_2$ fluxes.

2. Method

The method used in this study is a variation of the TransCom 3 Level 2 (T3L2) protocol (Gurney et al., 2000). The necessary change is the simulation of daily biospheric fluxes to capture as much as possible the synoptic atmosphere–biosphere interaction in the forward simulation. The models used in this study are the NIES atmospheric transport model and the Biome-BGC ecosystem model.

The NIES model (Maksyutov and Inoue, 2000) uses National Centers for Environmental Prediction (NCEP) reanalysis meteorology (Kalnay et al., 1996) to transport the atmospheric CO$_2$ concentrations resulting from the surface CO$_2$ fluxes. The model domain uses the latitude–longitude horizontal grid with a resolution of 2.5° × 2.5°. Vertically, the model has 15σ levels ranging from 0.985 to 0.065 (∼0.15 to ∼20 km in altitude, exact height depends on surface pressure). Time step in the model is 2 hr. The advection scheme is semi-Lagrangian with mass adjustment to conserve tracer mass. The planetary boundary layer (PBL) height in the model is specified with the monthly mean climatological PBL heights (from the Data Assimilation Office at NASA’s Goddard Space Flight Center). Besides the advection by vertical wind, two vertical mixing processes in the model are: (1) turbulent diffusion which is temperature dependent (stability function) and (2) cumulus convection derived from the humidity, temperature and wind fields (see Appendix A for details of vertical mixing processes). Although the PBL is specified with the climatological mean monthly values, these other vertical mixing processes can approximately represent the synoptic scale transport processes resolvable in the NCEP meteorology (particularly above the PBL) within a transport model.

The Biome-BGC model (Thornton et al., 2002) computes the daily ecosystem fluxes including net primary production (NPP), heterotrophic respiration (HR) and net ecosystem exchange (NEE) in response to atmospheric forcing such as temperature, humidity, precipitation and radiation. (See Fujita et al. (2003) for a detailed description of the model.) The model resolution is 1° × 1°, with a time step of 1 d. The meteorological forcing is the NCEP re-analysis meteorology. By using the same NCEP reanalysis meteorology in the Biome-BGC and NIES models, the CO$_2$ fluxes and CO$_2$ transport are mutually consistent. For example, under a cloudy cyclonic system, the solar radiation reaching the surface is reduced leading to the reduction of photosynthesis, resulting in the relatively enhanced CO$_2$ flux into the atmosphere; in turn this enhanced CO$_2$ flux is transported higher into the atmosphere by the more convective vertical motion. Thus, this model can capture the synoptic scale interaction between the atmosphere and the biosphere inherent in the NCEP data. As there is no constraint requiring these daily atmosphere–biosphere interactions to average to zero on the monthly or longer timescales, these interactions might have contributions to the monthly and annual CO$_2$ concentration fields and consequently on inversion flux estimates based on these CO$_2$ concentration fields. These effects are examined in the following forward and inverse modelling.

2.1. Forward simulation strategy

2.1.1. Daily and monthly CO$_2$ fluxes. The global 1° × 1° daily biospheric fluxes including NEE and NPP are simulated with the Biome-BGC model and the NCEP meteorology for the 10 yr period from 1990 to 1999. The daily NEE fluxes are adjusted to be annually neutral at every grid point each year. The adjustment consists of applying a minor constant correction to HR throughout the year. This adjusted NEE flux is referred to as the ‘daily
NEE flux.’ Next the daily NEE fluxes for each individual month over the 10 yr are averaged and are referred to as the ‘monthly mean NEE fluxes’. Thus, the monthly mean flux is comparable to the CASA flux used in the TransCom experiments.

2.1.2. Transport of atmospheric CO2 concentrations. Transport simulations consist of two cases referred to as the Reference and Synoptic Cases.

(i) **Reference Case:** simulate the transport of CO2 for 10 yr with the NIES model using NCEP winds from 1990 to 1999 and the monthly mean NEE flux repeated each year.

(ii) **Synoptic Case:** simulate the transport of CO2 for 10 yr with the NIES model using NCEP winds from 1990 to 1999 and the daily NEE flux from 1990 to 1999.

For the evaluation of model performance, the modelled atmospheric CO2 concentrations are shown in comparison to the observations at three sites in Appendix B. To examine the effects of the synoptic atmosphere–biosphere interaction, the presentation of results will focus on the differences in the CO2 concentrations between the two cases.

2.2. Inversion strategy

To quantify the effects of the synoptic atmosphere–biosphere interaction on inversion estimates, we repeat the time-dependent (for the period from 1992 to 1995) TransCom 3 monthly inversion (Baker et al., 2006) with the Biome-BGC monthly mean NEE fluxes (Reference Case, replacing the CASA fluxes used by TransCom 3) and compare the results to the inversion estimates obtained from the CO2 background field generated by the daily NEE fluxes (Synoptic Case). In this study, we used the same set of monthly station observed atmospheric CO2 concentration (78 sites) and their associated uncertainties from GLOBALVIEW-CO2 (2000) and Bayesian inversion program by Gurney et al. (2000). GLOBALVIEW is a data product that interpolates CO2 measurements by continuous analyser or biweekly flask samples into monthly interval, with an extrapolation procedure to fill the data gaps (GLOBALVIEW-CO2, 2000). The presentation of results will focus on comparing the differences in the CO2 flux estimates between the Reference and Synoptic Cases.

3. Results and discussion

3.1. Temporal evolution

In the inversions, typically monthly-averaged atmospheric CO2 concentration data from the forward simulations are used. Therefore, the monthly time-series of the modelled CO2 concentrations at a number of selected sites are examined in this section. The results shown are the difference of the monthly averaged CO2 concentration between the Synoptic and Reference Cases (referred to as ‘synoptic CO2 concentration anomalies’ or simply ‘CO2 anomalies’). Thus the monthly averaged CO2 concentration differences or anomalies represent the transported signal from the difference between the biospheric daily CO2 fluxes and the biospheric monthly CO2 fluxes. In short, this difference between the biospheric daily CO2 fluxes and the biospheric monthly CO2 fluxes will be referred to as the ‘synoptic biospheric flux anomalies’ or simply ‘flux anomalies’. By definition, these synoptic biospheric flux anomalies have daily flux variability but zero annual totals at every point in the model.

The results are strongly dependent on the relative distance to the synoptic source/sink region. Figure 1 shows the locations of the sites covering different cases ranging from within the source region to far remote sites (site descriptions are summarized in Table 1) where the time-series of the CO2 anomalies are shown in Fig. 2.

Far from the continental synoptic biospheric flux anomalies, sites like Mauna Loa (19.53°N, 155.58°W) and Cape Grim (40.68°S, 144.68°E) (Figs. 2a and b) have small monthly synoptic CO2 concentration anomalies. The maximum monthly CO2 anomaly amplitudes in the 10 yr period are 0.67 ppm at Mauna Loa and 0.4 ppm at Cape Grim. Their 10-yr mean monthly anomaly amplitudes are 0.17 ppm at Mauna Loa and 0.11 ppm at Cape Grim. At these remote sites, monthly averaging of the CO2 concentration effectively removes the transported signal from the synoptic biospheric flux anomalies.

Another group of background sites are characterized as being near the continental synoptic biospheric flux anomalies such as Alert (82.45°N, 62.52°W), Estevan Point (49.38°N, 126.55°W), Sable Island (43.93°N, 60.02°W) and Ryori (39.03°N, 141.83°E). The synoptic CO2 concentration anomalies evolutions at these sites are shown in Figs. 2c–f. The maximum monthly anomaly amplitudes in the 10 yr period are 2.2 ppm at Alert, 2.1 ppm at Estevan Point, 4.1 ppm at Sable Island and 2.1 ppm at Ryori. Their 10-yr mean monthly CO2 anomaly amplitudes are 0.38 ppm at Alert, 0.36 ppm at Estevan Point, 0.63 ppm at Sable Island and 0.44 ppm at Ryori. Sable Island shows the strongest monthly variations in this group of stations for both the maximum and average monthly amplitudes. While Ryori and Sable Island are at similar distances downwind from the Asia and North America continents, respectively, the Sable Island monthly CO2 anomalies are larger than at Ryori. The synoptic atmosphere–biosphere interaction on the monthly timescale at the east coast of North America is stronger than at the east coast of Asia. This result is consistent with the fact that, in the ecosystem map used in the Biome-BGC model, Eastern North America mainly consists of forest, while East Asia has grassland; the Biome-BGC results show that the productivity in Eastern North America is larger than that of East Asia.

The locations with the largest monthly averaged synoptic CO2 concentration anomalies are the continental sites. Fraserdale (49.88°N, 81.57°W) and Hegyhatsal (46.95°N, 144.68°E) are examples of such sites (Figs. 2g and h, respectively). The monthly CO2 anomalies have maximum amplitudes of 4.6 ppm at Fraserdale and 6.3 ppm at Hegyhatsal; while the average
Table 1. Observation sites selected for this study

<table>
<thead>
<tr>
<th>Index in Fig. 1</th>
<th>Site</th>
<th>Country</th>
<th>Latitude (°)</th>
<th>Longitude (°)</th>
<th>Altitude (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Background: remote sites</td>
<td>a Mauna Loa</td>
<td>U.S.A.</td>
<td>19.53 N</td>
<td>155.58 W</td>
<td>3397</td>
</tr>
<tr>
<td>b Cape Grim</td>
<td>Australia</td>
<td>40.68 S</td>
<td>144.68 E</td>
<td>94</td>
<td></td>
</tr>
<tr>
<td>Background: coastal sites</td>
<td>c Alert</td>
<td>Canada</td>
<td>82.45 N</td>
<td>62.52 W</td>
<td>210</td>
</tr>
<tr>
<td>d Estevan Point</td>
<td>Canada</td>
<td>49.38 N</td>
<td>126.55 W</td>
<td>500</td>
<td></td>
</tr>
<tr>
<td>e Sable Island</td>
<td>Canada</td>
<td>43.93 N</td>
<td>60.02 W</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>f Ryori</td>
<td>Japan</td>
<td>39.03 N</td>
<td>141.83 E</td>
<td>260</td>
<td></td>
</tr>
<tr>
<td>Continental</td>
<td>g Fraserdale</td>
<td>Canada</td>
<td>49.88 N</td>
<td>81.57 E</td>
<td>250</td>
</tr>
<tr>
<td>h Hegyhatsal</td>
<td>Hungary</td>
<td>46.95 N</td>
<td>16.65 E</td>
<td>258</td>
<td></td>
</tr>
</tbody>
</table>

The correlation analyses (not shown) of the synoptic biospheric flux anomalies to the synoptic CO₂ concentration anomalies at these continental sites show no significant correlations. This indicates that the synoptic CO₂ concentration anomalies are not strongly dependent on the local synoptic biospheric flux anomalies but are the result of the interaction of transport and flux/concentration. In Fig. 2, the following characteristics are evident at each site. They all have strong monthly and interannual variations. Occasionally, the CO₂ anomalies have longer durations of a few months. There is no apparent seasonal pattern in the signs of the CO₂ anomalies; they may be positive or negative throughout the years.

3.2. Spatial distribution

For some examples of the spatial CO₂ patterns, the global patterns of the monthly averaged surface CO₂ anomalies for January to December 1992 are shown in Fig. 3. The CO₂ anomalies have a wide range of spatial scales, from hundreds to thousands of kilometers. These CO₂ anomalies range from –5 to 7 ppm. The stronger CO₂ anomalies are typically centred on land and persist for one month or so. Occasionally the CO₂ anomalies persist for longer periods. For example, a strong negative CO₂ anomaly with large spatial extent over the Ural mountain region persists from January to March, and a strong positive CO₂ anomaly in almost the same area persists from July to September. In fact, this area has strong CO₂ anomaly patterns throughout the 10 yr of model simulation, reflecting the strong covariance of the atmospheric transport and the synoptic biospheric flux anomalies.

On the annual timescale, the spatial patterns of the annually averaged synoptic CO₂ concentration anomalies for 1992 and 1993 are shown in Fig. 4 as examples. The differences between these 2 yr represent typical interannual variations. Even when averaged annually, some anomaly patterns remain in the surface CO₂ concentration field. These CO₂ deviations range from –1 to 1.5 ppm. The spatial patterns are similar to the monthly CO₂ anomaly fields with strong anomalies centred over land regions. There are strong interannual variations in the annual patterns. These annual CO₂ anomaly patterns represent the time-mean
spatial CO₂ concentration gradient in the atmosphere resulting from the covariance of the CO₂ concentrations from the synoptic CO₂ flux anomalies and the atmospheric transport. Therefore it may be referred to as the synoptic Rectifier Effect, analogous to the seasonal Rectifier Effect (Denning et al., 1995) identified for the covariance of the CO₂ concentrations from the monthly mean CO₂ fluxes and transport. A note of caution is required here. Since this model may not fully capture all the synoptic and subsynoptic processes in the atmosphere and the biosphere, the results presented here may only be considered an approximation of the synoptic Rectifier Effect.

These results show the possible spatial and temporal range of atmospheric CO₂ variations in the biospheric background CO₂ concentration field with daily NEE fluxes compared to the standard biospheric background with monthly NEE fluxes.

3.3. Inversion

Using the biospheric fluxes from the Reference and Synoptic Cases, we can obtain two biospheric backgrounds usable in inversions. The biospheric background from the Synoptic case represents the CO₂ field with the Biome-BGC daily NEE fluxes. The inversion result using this biospheric background is referred to as the Synoptic Inversion. The biospheric background from the Reference Case represents the CO₂ field with the Biome-BGC monthly mean fluxes. The inversion result using this biospheric background is referred to as the Reference Inversion. The inversion procedure follows closely the time dependent inversion method for the monthly inversion of T3L2 (Baker et al., 2006). The main difference between the Reference Inversion and T3L2 is that the Reference Inversion in this study uses the Biome-BGC
monthly mean fluxes, while T3L2 used the CASA monthly fluxes. This substitution is to ensure better comparability to the Synoptic Inversion. The CASA monthly fluxes mutually consistent with NCEP meteorology for different years required by the Synoptic Case are not available from TransCom for this study.

The period of inversion in this study is from 1992 to 1995. The biospheric background for the Reference Inversion is produced with the monthly mean NEE fluxes according to T3L2. The biospheric background for the Synoptic Inversion is generated with the daily NEE fluxes. Thus, the synoptic biospheric background for year ‘n’ is produced by releasing the daily NEE fluxes generated by the NCEP meteorology of year ‘n’ into the transport model and integrated using the NCEP winds from years n, n + 1 and n + 2. Since the flux and transport vary interannually in the Synoptic Case, thus the ‘interannual variations in the rectification’ is also captured in the Synoptic Case but not in the Reference Case. The response functions are the same in both inversions to highlight the effects of the synoptic biospheric background on inversion results. Thus, monthly response functions are generated using the 10 yr annual mean spatial distributions of NPP for the different land regions with atmospheric transport driven by the 1993–1995 NCEP meteorological data. Note it is worthwhile in future studies to examine the possible difference in interannual inversion results if the response functions include spatiotemporal variations in CO2 flux patterns and interannual variations in the wind transport.
The global distribution of the annually average CO₂ concentration difference (Synoptic – Reference) for the year 1992 (a) and 1993 (b).

The monthly results from the two inversions for the 11 land and 11 ocean regions defined by TransCom 3 (see Fig. 1) are shown in Figs. 5 and 6, respectively. For the land regions, the monthly differences of the estimated fluxes between the Synoptic and Reference Inversion vary with time and regions. The maximum magnitude of the differences is $\sim 0.4$ GtC month$^{-1}$. Also, there are periods when the differences have the same sign for a few months. The region with the most frequent and significant
Fig. 5. The estimated monthly fluxes for the 11 land regions by the Reference (black line) and Synoptic inversions (black dotted line). A negative flux indicates uptake of CO$_2$ by the land. Also shown is the prior flux from the neutral biosphere (grey line).

The monthly fluxes are summed to yield annual inverse fluxes. The results for the 11 land and 11 ocean regions are shown in Figs. 7 and 8, respectively. The uncertainties in the annual flux estimates for the Reference Inversion are also shown in the figures; the uncertainties are very similar for the Synoptic Inversion and are omitted in the monthly results to maintain the clarity of the figures. The results show that annually there are differences among the regions. Figure 7 shows that the land regions Tropical Africa and Australia have minimal differences between the two inversions. The other land regions show larger differences and more temporal variability, including Europe which displays differences throughout the time period. The ocean regions in Fig. 8 display a similar range of differences between the two inversions. However, as noted above, South Pacific shows persistent and the largest differences of the same sign during the period. The difference between the two inversions can be as large as 0.5 GtC yr$^{-1}$. This may be a reflection of the poorly constrained nature of the region.

The annual results for all the land and ocean regions are summed to yield a global inversion flux estimate for each
The estimated monthly fluxes for the 11 ocean regions by the Reference (black dotted line) and Synoptic Inversions (black line). A negative flux indicates uptake of CO₂ by the ocean. Also shown is the prior flux from the ocean (grey line).

Table 2. The global land, ocean and total (land + ocean) inverse flux estimates for 1992–1995 for the Reference, Synoptic and their difference (GtC yr⁻¹)

<table>
<thead>
<tr>
<th>Year</th>
<th>Reference Inversion</th>
<th>Synoptic Inversion</th>
<th>Difference (Synoptic – Reference)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Land</td>
<td>Ocean</td>
<td>Total</td>
</tr>
<tr>
<td>1992</td>
<td>–2.00</td>
<td>–2.81</td>
<td>–4.81</td>
</tr>
<tr>
<td>1993</td>
<td>–2.02</td>
<td>–1.28</td>
<td>–3.30</td>
</tr>
<tr>
<td>1994</td>
<td>0.73</td>
<td>–2.68</td>
<td>–1.95</td>
</tr>
<tr>
<td>1995</td>
<td>1.03</td>
<td>–3.31</td>
<td>–2.28</td>
</tr>
</tbody>
</table>

The annual uncertainties have very minor variations during these years; the uncertainties are ±1.5 GtC yr⁻¹ and ±0.5 GtC yr⁻¹ for the global land and ocean, respectively. The uncertainties are similar for both the Reference and Synoptic Cases.

The results are summarized in Table 2. For the Reference Inversion, the results show large interannual variability for both land and ocean. The ranges of variation are 3.05 GtC yr⁻¹ for land, 2.03 GtC yr⁻¹ for ocean and 2.86 GtC yr⁻¹ for the total (land + ocean). By including the synoptic biospheric variations, the inversion results show larger interannual variations for both land and ocean. The ranges are 3.39 GtC yr⁻¹ for land, 2.26 GtC yr⁻¹ for ocean and 2.83 GtC yr⁻¹ for the total. These results represent 11% increases for both land and ocean, but a 1% decrease for the total.
For the individual years, there are large changes in fluxes both in magnitude and percentage. The largest difference in the land flux is 0.44 GtC yr\(^{-1}\) in magnitude (1993) and 22% in percentage (1993). The largest difference in the ocean flux is 0.48 GtC yr\(^{-1}\) in magnitude (1993) and 37% in percentage (1993). For the total of land and ocean, the largest difference is 0.16 GtC yr\(^{-1}\) in magnitude (1995) and 7% in percentage (1995). The pattern of increment of uptake for land and reduction of uptake for ocean persists throughout this 4 yr period. The average land sink increased by 0.19 GtC yr\(^{-1}\) and the average ocean sink decreased by 0.30 GtC yr\(^{-1}\).

Another overall measure of the difference from neglecting the synoptic variability in the biospheric background fluxes (referred to as between-methods difference) can be represented by the root mean square of the monthly differences of flux estimates between the two inversions. The results for the 22 regions are shown in Table 3. For comparison, Table 3 also included the posterior uncertainties (mean of the Synoptic and Reference Cases) for this study, as well as the ‘within-model’ uncertainties and ‘between-model’ uncertainties from Gurney et al. (2004). The posterior uncertainties in this study are similar to the ‘within-model’ uncertainties, indicating that the uncertainties are comparable (some of the differences between the posterior uncertainties of this study and the TransCom ‘within’ uncertainties might be the result of the inversions with different CO\(_2\) observation sites, different time period of inversion, cyclostationery compared to time dependent and different biospheric fluxes). The region with the largest between-methods difference (1.65 GtC yr\(^{-1}\)) is Europe, the region with strong synoptic variations compared to the Reference Case. This between-methods difference is about four times larger than the other uncertainties in Table 3. The other regions with about two times larger between-methods difference than the other uncertainties are Boreal North America, Temperate North America, Boreal Asia

Fig. 7. The estimated annual fluxes for the 11 land regions by the Reference (black dotted line) and Synoptic Inversions (black line). A negative flux indicates uptake of CO\(_2\) by the land.
4. Conclusions

The sparseness of CO₂ concentration observations makes atmospheric CO₂ inversion an underconstrained problem. The Bayesian inversion commonly used for CO₂ inversion includes many assumptions and approximations. Each assumption or simplification introduces uncertainties in the inversion results. This study examined the approximation that the biospheric fluxes have a smooth monthly variation. The spatiotemporal effects of sub-monthly or synoptic biospheric variations were studied by using the NIES transport model to simulate the cases of biospheric fluxes from the Biome-BGC model with and without synoptic variations. Then Bayesian inversion analyses were performed to estimate the effects of the synoptic atmosphere–biosphere interaction on regional flux estimates.

The spatiotemporal characteristics of the synoptic atmosphere–biosphere interaction were computed from the difference between the two simulations. Temporally, the synoptic biospheric flux anomalies did not average to zero and were present in the monthly and annually averaged atmospheric CO₂ concentrations. The synoptic CO₂ anomalies showed strong monthly and interannual variability. The magnitude of the synoptic CO₂ concentration anomalies was shown to be a strong function of the distance from the continental biospheric source regions.

On the monthly timescale, a remote site like Mauna Loa showed averaged monthly amplitude of 0.2 ppm with maximum amplitude of 0.7 ppm. Coastal sites showed averaged monthly amplitudes of 0.4–0.6 ppm, with maximum amplitudes of...
Table 3. The between-methods differences of flux estimate and the mean posterior uncertainties in the reference and synoptic inversions (GtC yr\(^{-1}\))

<table>
<thead>
<tr>
<th>Land regions</th>
<th>Between-methods difference (this study)</th>
<th>Mean posterior uncertainty (this study)</th>
<th>“Between” Uncertainty (Gurney et al., 2004)</th>
<th>“Within” Uncertainty (Gurney et al., 2004)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Boreal North America</td>
<td>0.80</td>
<td>0.27</td>
<td>0.28</td>
<td>0.18</td>
</tr>
<tr>
<td>Temperate North America</td>
<td>0.73</td>
<td>0.24</td>
<td>0.32</td>
<td>0.22</td>
</tr>
<tr>
<td>Tropical America</td>
<td>1.20</td>
<td>0.61</td>
<td>0.77</td>
<td>0.73</td>
</tr>
<tr>
<td>South America</td>
<td>0.64</td>
<td>0.60</td>
<td>0.61</td>
<td>0.64</td>
</tr>
<tr>
<td>Tropical Africa</td>
<td>0.79</td>
<td>0.53</td>
<td>0.85</td>
<td>0.54</td>
</tr>
<tr>
<td>South Africa</td>
<td>0.84</td>
<td>0.66</td>
<td>0.60</td>
<td>0.58</td>
</tr>
<tr>
<td>Boreal Asia</td>
<td>1.02</td>
<td>0.33</td>
<td>0.51</td>
<td>0.23</td>
</tr>
<tr>
<td>Temperate Asia</td>
<td>1.02</td>
<td>0.36</td>
<td>0.74</td>
<td>0.34</td>
</tr>
<tr>
<td>Tropical Asia</td>
<td>0.89</td>
<td>0.43</td>
<td>0.94</td>
<td>0.45</td>
</tr>
<tr>
<td>Australia</td>
<td>0.23</td>
<td>0.13</td>
<td>0.15</td>
<td>0.14</td>
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The between-methods differences are the root mean square of monthly flux estimate differences between the reference and synoptic inversions. For comparison, ‘Between-model’ and ‘Within-model’ Uncertainties from the seasonal inversion study of TransCom 3 Level 2 (Gurney et al., 2004) are listed.

2–4 ppm. Continental sites showed averaged monthly amplitudes of 1-2 ppm with maximum monthly amplitude exceeding 6 ppm. Spatially, the monthly CO\(_2\) anomaly patterns with amplitudes up to \(\sim 7\) ppm were shown to have typical length scales from a few hundred to a thousand kilometers. The CO\(_2\) anomalies were centred over land regions. On the annual timescale, the spatial patterns were similar to the monthly patterns but the maximum CO\(_2\) anomaly amplitude was reduced to \(\sim 1.5\) ppm. These simulated synoptic CO\(_2\) anomaly patterns were the results of the interaction of the synoptic CO\(_2\) anomalies field and atmospheric transport, and were defined as the synoptic Rectifier Effect.

Two sets of inversion CO\(_2\) fluxes were obtained following the TransCom3 level 2 time dependent method using biospheric background fields with and without synoptic biospheric flux variations. The 22-region monthly inversions were performed for the years 1992 to 1995. Comparisons showed that the synoptic Rectifier Effect on inversion varied in space and time. Monthly inversion differences were larger for the land regions than for the ocean regions. The maximum magnitude of the differences was \(\sim 0.4\) GtC month\(^{-1}\) for the land regions and \(\sim 0.2\) GtC month\(^{-1}\) for the ocean regions. In the 4 years of inversion results, the Synoptic Inversion showed 11% greater range of interannual variations for the annual land and ocean fluxes compared to the Reference Inversion.

These results are dependent on the models used. There are numerous approximations that could affect the simulation results of the synoptic interaction between the biosphere and atmosphere. These approximations include: prescribed PBL and low spatial resolution in the transport model, low temporal resolution in the NCEP meteorological data, and the lack of diurnal variation in the biospheric fluxes from the Biome-BGC model. Other important factors in the simulation of the atmosphere–biosphere interaction include the accuracy of the synoptic biospheric flux simulation, and the accuracy of the NCEP wind field data. Inversion results could be influenced by factors including coarse model resolution in space and time, observational data (quality, space-time resolution and processing). Capturing more atmosphere–biosphere interactions including the synoptic variations of the PBL and subsynoptic scale interactions might result in a stronger synoptic Rectifier compared to this study. If
the atmosphere–biosphere interactions are adequately simulated in the model and represent a more realistic state of the atmospheric CO\textsubscript{2} spatiotemporal distribution, then the results of this study suggest that properly designed inversion procedure may yield improved flux estimates by the inclusion of the synoptic atmosphere–biosphere interactions.

5. Acknowledgments

We thank Christian Rödenbeck for helpful comments on this manuscript. We are grateful for the constructive comments and suggestions by the two anonymous reviewers on our submission which have greatly helped to improve this manuscript. This work is partially funded by the Canadian Foundation for Climate and Atmospheric Sciences.

6. Appendix A

Two vertical mixing processes are represented in the model: (1) turbulent diffusion which is temperature dependent (stability function) and (2) cumulus convection derived from the humidity, temperature and wind fields.

A.1. Turbulent diffusion

Below PBL top, the turbulent diffusivity is set to constant value of 40 m\textsuperscript{2} s\textsuperscript{-1}. Above PBL, the turbulent diffusivity ($K$) is calculated using local stability function following Hack et al. (1993):

$$K = l^3S_F(Ri), \quad (A1)$$

where

\[ l = 30 \text{ m} \quad \text{: mixing length} \]

\[ S = \left| \frac{\rho g}{P_i} \frac{\partial V}{\partial \sigma} \right| \quad \text{: vertical wind shear} \]

\[ F_s(Ri) \quad \text{: stability dependent function} \]

\[ Ri = -\frac{\rho g^2}{P_i} \left( \frac{1}{S^2} \frac{\partial \ln \theta_v}{\partial \sigma} \right) \quad \text{: local Richardson number which is a function of the virtual potential temperature($\theta_v$) and acceleration of gravity ($g$).} \]

$F_s(Ri)$ is defined as:

\[ F_s(Ri) = (1 - 18Ri)^{1/2} \quad (Ri < 0). \]

\[ F_s(Ri) = 1 - \frac{Ri}{Ri_c} \quad (0 < Ri < Ri_c = 0.2). \]

\[ F_s(Ri) = 0 \quad (Ri > Ri_c = 0.2). \]

A.2. Cumulus convection

The cumulus convection in the model is based on cumulus mass-fluxes calculated in a Kuo-Type scheme described in Grell et al. (1995). The model also includes entrainment and detrainment processes on convective updrafts and downdrafts in the form proposed by Tiedtke (1989). In the model, the convective rates are determined in the following steps:

1) The cloud base level $\sigma_c$ is obtained by adding small perturbation humidity and temperature to levels below the $\sigma$ level corresponding to 700 hPa and adiabatically lifting the air parcel until the condensation occurs. The cloud base $\sigma_c$ is set to the lowest level where condensation would occur.

2) The supply rate of moisture available for penetrative convection is then estimated. The horizontal moisture divergence is evaluated from winds and water vapour content. Low-level moisture convergence $M_l$ is obtained by integrating the horizontal moisture convergence below cloud base level:

$$M_l = -\int_{\sigma_c}^{1} \nabla_s (p_s \nabla q) d\sigma - M_C + S_{\text{evap}}. \quad (A2)$$

where $S_{\text{evap}}$ is surface evaporation. To account for deviation from the mass conservation in the wind data, the moisture divergence term is corrected for non-zero divergence of the air mass $M_C$:

$$M_C = \int_{\sigma_c}^{1} q \nabla_s (p_s \nabla) d\sigma. \quad (A3)$$

Several criteria are checked to exclude grid cells with no significant deep cumulus convection following Grell et al. (1995).

3) The mass flux $M_u$ in updraft is set to $M_l$ divided by water vapour mixing ratio at cloud base $q_{\text{base}}$, so that $M_l = M_u q_{\text{base}}$. The vertical profiles of entrainment and detrainment rates are set to be proportional to $M_u$, in accordance with Tiedtke (1989). In the updraft air, virtual potential temperatures are evaluated from the cloud base level to the cloud top level. The cloud top is determined by comparing the virtual potential temperatures in the updraft and environment, for which an overshoot of 3 K is allowed.

4) The cloud with thickness of thinner than $\Delta \sigma = 0.1$ are excluded. The downdraft mass flux is set 0.2 of that in the updraft, same as in Tiedtke (1989).

5) The tracers are transported vertically by applying a simplified explicit scheme. It is assumed that the updraft and downdraft make only a negligibly small part of a grid column; the rest is designated as environment air. First the vertical profiles of the concentrations in the updraft and downdraft air are computed by taking into account rates of mixing with environment air by entrainment and detrainment, and then the concentration...
tendencies in environment air are obtained from the entrainment/detrainment rates.

7. Appendix B

B.1. Model performance in simulating atmospheric CO$_2$

Using the NIES transport model and the Biome-BGC biospheric flux model, the forward simulations for the case of daily varying Biome-BGC flux and the case of monthly varying Biome-BGC flux were done. Before comparing the difference between these two simulations at a series of CO$_2$ measurement sites, it is useful to show how the model simulated CO$_2$ concentrations compare with observations at the measurement sites. There are only a limited number of sites with continuous CO$_2$ concentration measurements necessary for this comparison in the period 1990–1999. In this section, a comparison of the two simulations to observations at three measurement sites representing the three different types of sites discussed in this study is presented. The three sites are Mauna Loa (a background site far from continental biospheric sources), Alert (a background site near the continent) and Fraserdale (a continental site). The observational data we have used are from two sources: Mauna Loa from National Oceanographic and Atmospheric Administration/Climate Monitoring and Diagnostics Laboratory (NOAA/CMDL, USA) (Thoning et al., 1989), Alert and Fraserdale from Meteorological Service of Canada (MSC) (Trivett and Higuchi, 1989; Higuchi et al., 2003).

Figure 9 shows the time-series of simulated atmospheric CO$_2$ concentrations with the Biome-BGC monthly and daily CO$_2$ fluxes (corresponding to Reference and Synoptic Cases) at Mauna Loa, Alert and Fraserdale along with the observational results. The modelled and observational results are detrended, by subtracting the long-term components through the digital filtering method (Nakazawa et al., 1997). The time-series of the observations are composed of only measurements in the afternoon, when PBL is well developed and CO$_2$ signals are well mixed inside the PBL. The modelled CO$_2$ concentrations capture the overall seasonal cycles. There is no significant difference of the modelled atmospheric CO$_2$ with daily and monthly fluxes at Mauna Loa and Alert, while there are notable differences between the two cases in the growing seasons at Fraserdale. The model simulation result with the monthly biospheric fluxes shows less synoptic variability than that with the daily.

For a more quantitative comparison of how well the model can simulate the observed variability, the standard deviations (as the measure of variability) of the monthly CO$_2$ concentration for
Fig. 10. The 10-yr averaged monthly standard deviations of simulated atmospheric CO$_2$ concentrations at Mauna Loa, Alert and Fraserdale for Reference and Synoptic Cases, along with the observations.

The two simulations and observations are computed. Then each month’s standard deviations (SD) are averaged over 10 yr (1990–1999) to minimize data problem such as missing data. Figure 10 shows the 10-yr averaged monthly SDs of simulated and observed CO$_2$ concentration for Mauna Loa, Alert and Fraserdale.

For Mauna Loa, the SDs for the Reference and Synoptic Cases are nearly equal and both SDs are similar to the SD for the observation. The model SDs are very slightly larger than the SD of the observation in the winter, and smaller than the observation SD in August to October, capturing only about 50% of the observed variability.

For Alert, the SDs for the Reference and Synoptic Cases are nearly equal in the winter. While in the growing season (June–October), the SD for the Synoptic Case is about 10% larger than the Reference Case. Comparing to the observation SD, the model SDs are too large in the winter and spring, up to ~200% larger in March. In the growing season, the observation SD is larger than the model SDs, as the model SDs can capture about 40–70% the observation SD. The large SD in the model CO$_2$ concentration appears to be caused by too much winter respiration signals.

Fraserdale results show much more difference between the Reference and Synoptic Cases. In the winter (December, January and February), the model SDs are very similar to each other and both are larger than the observation SD (similar to Alert). Then from April to October, the Synoptic Case SD is significantly larger than the Reference Case SD. The Reference case SD is only about 50% as large as the Synoptic Case SD between April to July. In August and September, the difference in the SDs is quite large, the Reference case is capturing only about 15–30% of the Synoptic Case. The Synoptic SD appears to be much closer to the observation SD than the Reference SD.

These results show that the model can simulate the seasonal cycle reasonably at the different measurement sites. The variability is simulated better in the Synoptic Case than the Reference Case at the continental site. In this study, the difference between the Synoptic and Reference Cases are examined in both forward and inverse modelling.

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